

1. **(Rotational motion – kinematics/dynamics, 5/ea.)** A force of 50 N exerts on 10-kg uniform disk with a radius $R = 0.2$ m for 1 second time period to initiate ($t = 0$) spinning of the disk. Assumption: frictionless.

Disc of Mass M
Axis of Rotation
R/2
R
F

(a) What is the torque applied to the disk? **Ans.** _____ 10 N.m.
 (b) What is the angular acceleration during the first 1-second period? **Ans.** _____ 50 rad./s²
 (c) What is the angular velocity when $t = 1$ s? **Ans.** _____ 50 rad./s
 (d) What is the total rotated angle during the first 1-second? **Ans.** _____ 25 rad.
 (e) What is the total rotated angle during the second 1-second time period? **Ans.** _____ 50 rad.

2. **(Rotational motion – dynamics/energetics, 5/ea.)** Refer to the problem #1 (**double-check your results in the first problem**), find:

Refer to the diagram in 1.	(a) the work done by the torque. Ans. _____ 250 J (b) the rotational kinetic energy at the end of the first 1 s. Ans. _____ 250 J (c) the angular momentum at the end of the first 1 s. Ans. _____ 10 kg.m ² /s If a point-mass with mass of 5 kg is adhered to the disk at $r = R/2$ as shown at the end of first 1 s, find: (d) the rotational inertia for the disk with the point-mass? Ans. _____ 0.25 kg.m ² , and (e) the new angular velocity assuming the angular momentum is conserved? Ans. _____ 40 rad./s
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3. **(Oscillatory motion: spring with a point-mass, 5/ea.)** A 1-kg point-mass with zero initial velocity connected with a spring is being displaced by $X_m = 0.15$ m. Assume (1) the force constant of the spring (K) is 9 N/m, and (2) the motion of spring/object is frictionless and $t = 0$ when the point-mass is at $x = 0$ m.

$v = 0$
F
k
m
 $x = 0$ $x = X$

(a) What is the oscillation period of the point-mass, T ? **Ans.** _____ 2.1 s
 (b) What is the oscillation frequency of the point-mass? **Ans.** _____ 0.5 Hz
 (c) What is value of $x(t)$ for $t = 2T$? **Ans.** _____ 0
 (d) What is the maximum kinetic energy of the point-mass? **Ans.** _____ 0.1 J
 (e) What is the work done by the spring-force when the point-mass is being displaced from X to the origin $x = 0$? **Ans.** _____ 0.1 J

4. **(Oscillatory motion: pendulum, 5/ea.)** A pendulum system with $L = 1$ m and $m = 2$ kg is initially energized by giving a potential energy of 0.2 J to the system. Assumption: frictionless, $g = 9.8$ m/s²

θ
L
T
m
 $-mg \sin \theta$
 $w = mg$

(a) What is the maximum kinetic energy of the point-mass? **Ans.** _____ 0.2 J
 (b) What is the maximum velocity of the point-mass (magnitude only)? **Ans.** _____ 0.45 m/s
 (c) What is the maximum displacement of the point-mass, S_m ? **Ans.** _____ 0.14 m
 (d) What is the maximum force exerts on the point-mass? **Ans.** _____ 2.7 N
 (e) What is the net force exerts on the point-mass when it has the maximum velocity? **Ans.** _____ 0

<Equations given below are for your reference only>

Rotational motion	$I = (1/2)mr^2$ for uniform disk	$I = mr^2$ for a point mass		
	$\theta = \theta_0 + \omega_0 \Delta t + (1/2)\alpha \Delta t^2$ $\omega = \omega_0 + \alpha \Delta t$	$\tau = Fr$; $L = I\omega$	$\tau = I\alpha$; $W = \tau \Delta \theta$	$KE_{rot} = (1/2) I \omega^2$
Oscillatory motion – spring with a point-mass	$F = -Kx$; $F = ma$ $\omega = (K/m)^{1/2}$	$x(t) = X_m \sin(\omega t)$; $v(t) = X_m \omega \cos(\omega t)$;	$a(t) = -X_m \omega^2 \sin(\omega t)$	$PE_m = (1/2)kX^2$; $KE_m = (1/2)mv_m^2$
Oscillatory motion -- pendulum	$\omega = (g/L)^{1/2}$	$s(t) = S_m \sin(\omega t)$; $v(t) = S_m \omega \cos(\omega t)$;	$a(t) = -S_m \omega^2 \sin(\omega t)$	